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**Spectral-linear and spectral-differential methods
for generating S-boxes having almost optimal
cryptographic parameters**

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Abstract. S-boxes are important parts of modern ciphers. To construct S-boxes having cryptographic parameters close to optimal is an unsolved problem at present time. In this paper some new methods for generating such S-boxes are introduced.

Keywords: S-box, substitution, involutory substitution, spectral-linear method, spectral-differential method, Kuznechik, BelT, Skipjack, Khazad-0, Khazad, Anubis

Спектрально-линейный и спектрально-дифференциальный методы построения S-боксов с близкими к оптимальным значениями криптографических параметров

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Аннотация. S-боксы являются важным элементом современных шифрсистем. Задача построения S-боксов с близкими к оптимальным значениями криптографических параметров в настоящее время не решена. В статье предлагается ряд новых методов построения таких S-боксов.

Ключевые слова: S-бокс, подстановка, инволютивная подстановка, спектрально-линейный метод, спектрально-дифференциальный метод, Кузнечик, BelT, Skipjack, Khazad-0, Khazad, Anubis

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